

7.  $V: (-2, 5)$  Pt:  $(0, 9)$

$$\begin{array}{c} \uparrow \uparrow \\ h \quad k \end{array}$$

Vertex form  $y = a(x-h)^2 + k$

$$\begin{array}{c} \uparrow \\ \text{missing} \end{array}$$

plug in all info :  $9 = a(0+2)^2 + 5$

solve for  $a$  :  $9 = a(2)^2 + 5$

$$9 = a \cdot 4 + 5$$

$$4 = a \cdot 4$$

$$1 = a$$

Vertex form

w/  $a, h, k$  plugged in : 
$$y = (x+2)^2 + 5$$

8.  $f(x) = 10000 - 110x + 45x^2$

minimum = vertex

$$h = \frac{-b}{2a} = \frac{-110}{2(45)} = \frac{110}{9} = 12.22 \text{ units (123 rounded)}$$

to produce Min. cost.

9.  $f(x) = 2x^5 + 24x^4 - 10x^2 + 5x - 3$

positive odd  $\Rightarrow$   $\cup$

left:  $-\infty$  (down)  
Right:  $\infty$  (up)

10.  $f(x) = 2x^8 - 12x^7 + 3x^4 + 5x^3 + 2x + 4$

positive even  $\Rightarrow$   $\cup$

Left:  $\infty$  (up)  
Right:  $\infty$  (up)

11.  $f(x) = x^3 - 4x^2 + 4x$  (zeros = x-int, #'s that make equation zero)

$$0 = x^3 - 4x^2 + 4x$$

$$0 = x(x^2 - 4x + 4)$$

$$0 = x(x-2)(x-2)$$

$$\uparrow \quad \uparrow \quad \uparrow$$

$$x=0 \quad x=2 \quad x=2$$

12. 
$$\begin{array}{r} x^2 + 2x + 4 \\ x^2 - 2x + 3 \\ \hline -4x^2 + 8x - 11 \end{array} + \frac{2x-11}{x^2 - 2x + 3}$$

$$\begin{array}{r} x^4 + 0x^3 + 3x^2 + 0x + 1 \\ -x^4 + 2x^3 - 3x^2 \\ \hline 2x^3 + 0x^2 + 0x + 1 \\ -2x^3 + 4x^2 - 6x \\ \hline 4x^2 - 6x + 1 \\ -4x^2 + 8x - 11 \\ \hline 2x - 11 \end{array}$$

13.

$$\begin{array}{r} 3x + 6 + \frac{13}{x-3} \\ x-3 | 3x^2 - 3x - 5 \\ -3x^2 + 9x \\ \hline 6x - 5 \\ -6x + 18 \\ \hline 13 \end{array}$$

14.

$$\begin{array}{r} 2 | 9 & -18 & -16 & 32 \\ & \downarrow & 18 & 0 & -32 \\ & 9 & 0 & -16 & 0 \end{array}$$

$$9x^2 + 0x - 16 \Rightarrow 9x^2 - 16$$

15.

$$\begin{array}{r} 2 | 5 & 3 & -4 & -4 & 4 & 6 \\ & \downarrow & 10 & 26 & 44 & 80 & 168 \\ & 5 & 13 & 22 & 40 & 84 & 174 \end{array}$$

$$5x^4 + 13x^3 + 22x^2 + 40x + 84 + \frac{174}{x-2}$$

16. Find one zero from Graphing